

Modelando objetos autogravitantes

```
> restart:with(plots):
```

A partir de una ecuación de estado politrópica, encuentro la función densidad

```
> rho:= exp((ln((P(r))/(K)))/(gamma1));
```

$$\rho := e^{\frac{\ln\left(\frac{P(r)}{K}\right)}{\gamma^I}} \quad (1)$$

Las ecuaciones de estructura para el caso newtoniana isotrópico serán

```
> Ecuac1 := diff(P(r),r) + m(r)*rho/r^2=0;
```

$$Ecuac1 := \frac{d}{dr} P(r) + \frac{m(r) e^{\frac{\ln\left(\frac{P(r)}{K}\right)}{\gamma^I}}}{r^2} = 0 \quad (2)$$

```
> Ecuac2 := diff(m(r),r) = 4*Pi*r^2*rho;
```

$$Ecuac2 := \frac{d}{dr} m(r) = 4 \pi r^2 e^{\frac{\ln\left(\frac{P(r)}{K}\right)}{\gamma^I}} \quad (3)$$

Defino los parámetros de mi ecuación de estado

```
> K := 1.5; gamma1 := 4/3;
```

$$K := 1.5$$

$$\gamma^I := \frac{4}{3} \quad (4)$$

y los parámetros de ejecución

```
> r0 := 10^(-4); ifinal:= 100; infinito := 10^(20):
```

$$r0 := \frac{1}{10000}$$

$$ifinal := 100 \quad (5)$$

Se plantea la integración del sistema de ecuaciones de estructura y se varía la condición inicial para la presión central.

```
> for i from 1 to ifinal do
# se define el sistema de ecuaciones
SistemaPm := {Ecuac1, Ecuac2, P(r0)= 1+5*i, m(r0)=0.}:
funcionesPm := {P(r),m(r)}:
#Se integra el sistema de ecuaciones para condiciones iniciales
variable en la presión
solucion:= dsolve(SistemaPm,funcionesPm,numeric,events=[[P(r)=10^
(-18),halt]],output=listprocedure):
# se almacena los valores resultados de la integración
radio := rhs(solucion[1]):presion := rhs(solucion[2]):masa := rhs
(solucion[3]):
# se captura el último valor de la masa, generando una queja del
sistema que desatendemos
masaTotal[i]:=masa(infinito):RadioExt[i]:=radio(infinito): Pnula[i]
:=presion(infinito):
# a partir del valor de la presión central se calcula el densidad
central
rho0[i]:= evalf(subs(P(r)=presion(r0),rho));
end do:
```

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Grafico los valores para puntos rhoCentral, masa total

```
> puntosMasarho0:= {seq([rho0[i],masaTotal[i]],i=1..ifinal)}:  
> pointplot(puntosMasarho0);
```

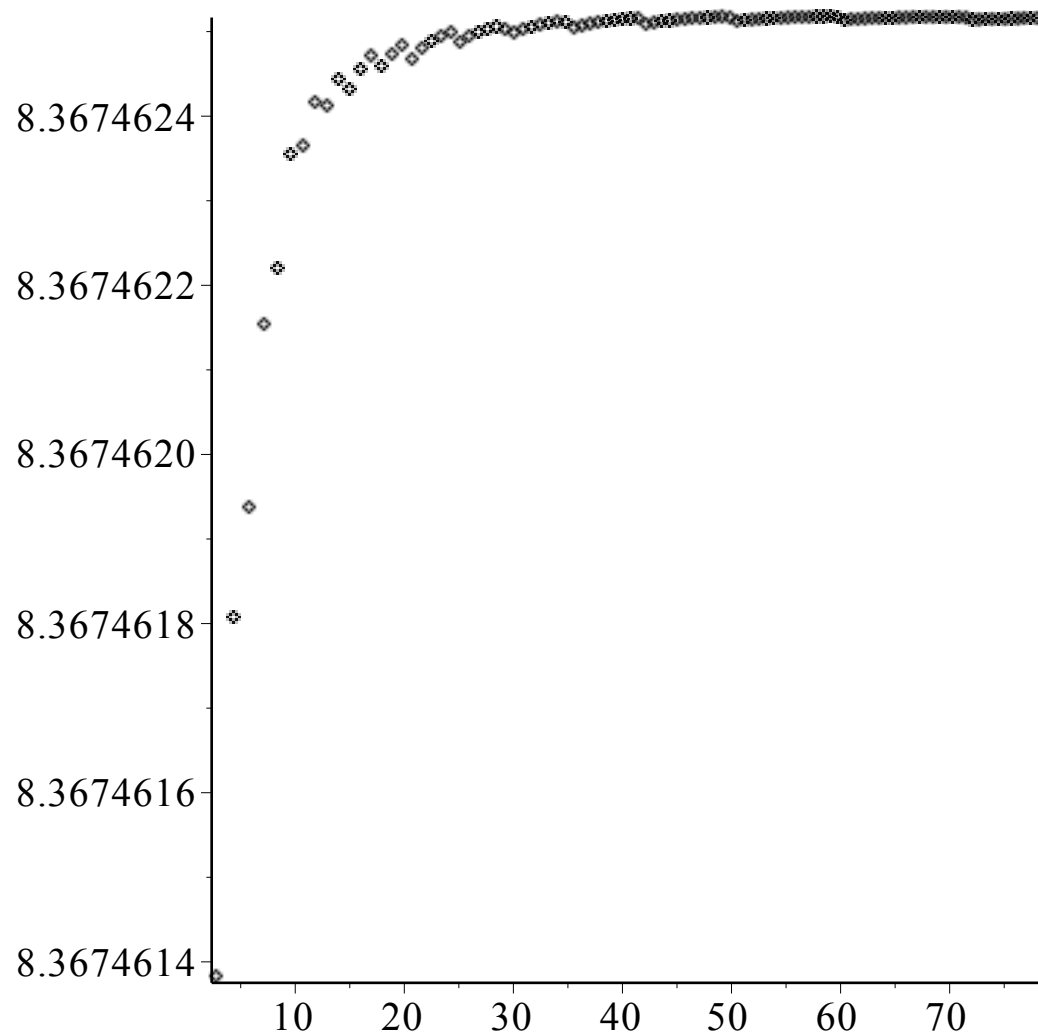


Grafico los puntos Radio exterior, masa total

```
> puntosMasaRadio:= {seq([RadioExt[i],masaTotal[i]],i=1..ifinal)}:  
> pointplot(puntosMasaRadio);
```

